

The Semantics of Partial Model Transformations

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Introduction: Uncertainty

Uncertainty: pervasive in SE

Introduction

Partial Models

Transforming Partial Models

Lifted Transform Semantics

Checking Lifted Rules

Conclusion

Models with uncertainty:

- Represent choice among many possibilities
- Can be refined to many different classical models

Our goal:

Handle models with uncertainty in MDE
without having to remove uncertainty.

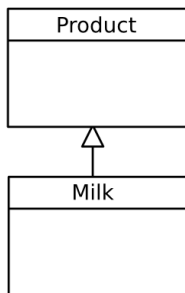
In this talk: Transformations of models with uncertainty

Introduction: Transformations

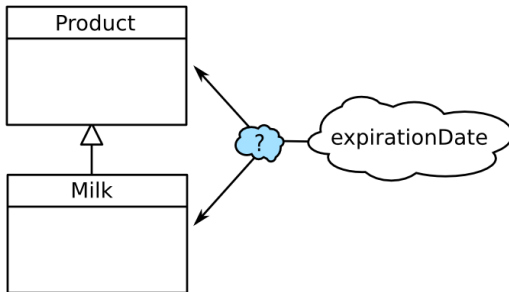
Existing model (graph) transformations:

- Unambiguous model is assumed as input.
- When model contains uncertainty:
 - either first remove uncertainty
 - Premature commitment.
 - Reduced quality.
 - or transform *all* alternatives.
 - Hard to maintain.

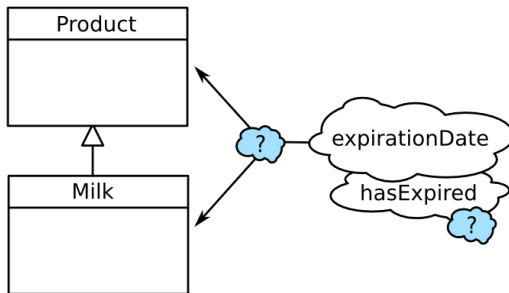
Motivating Example



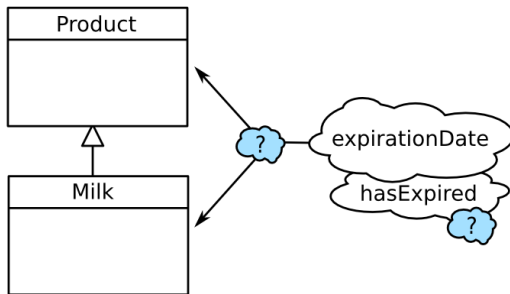
Motivating Example



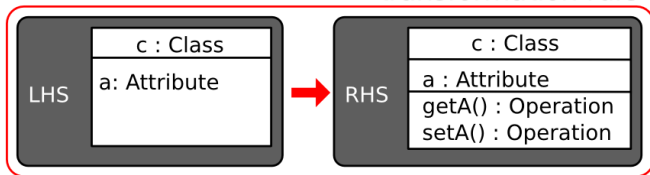
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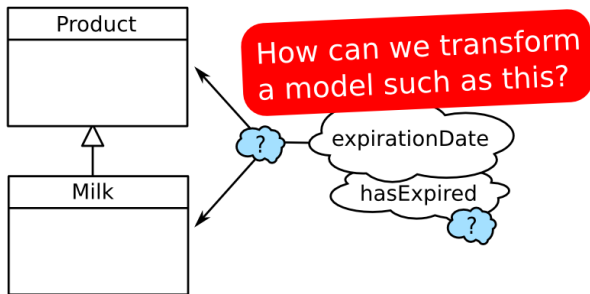
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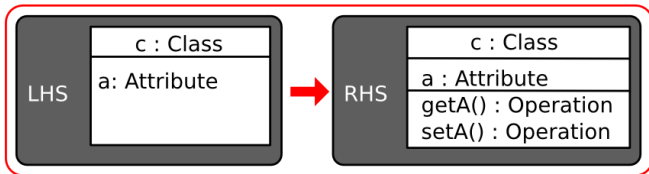
transformation rule



Motivating Example



transformation rule



① Introduction

② Partial Models

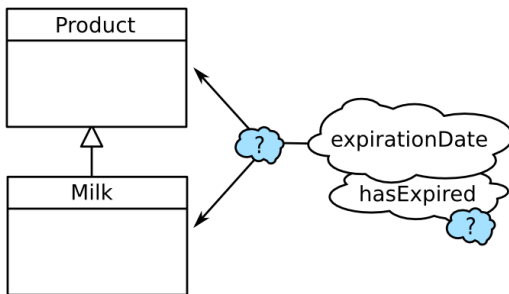
③ Transforming Partial Models

④ “Lifted” Transformation Semantics

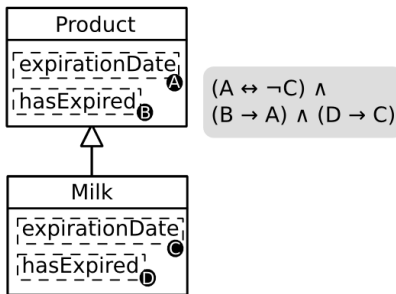
⑤ Checking Lifted Rules

⑥ Conclusion

Partial Models



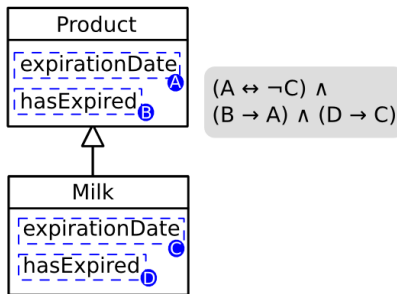
Partial Models



Partial Models:

- Explicate uncertainty
- Syntactic annotations [FASE'12]

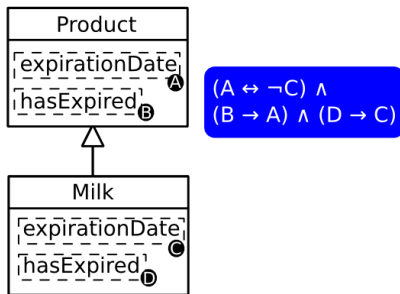
Partial Models



Partial Models:

- Explicate uncertainty
- Syntactic annotations [FASE'12]
- **Optional** / mandatory elements

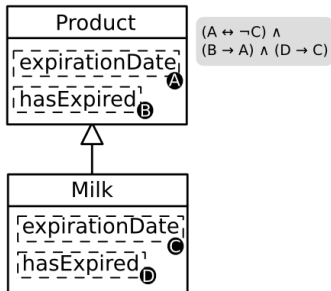
Partial Models



Partial Models:

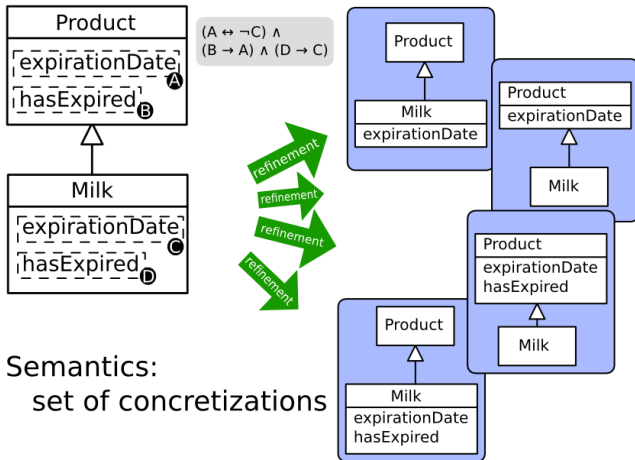
- Explicate uncertainty
- Syntactic annotations [FASE'12]
- Optional / mandatory elements
- **May formula** → allowable configurations

Semantics of Partial Models



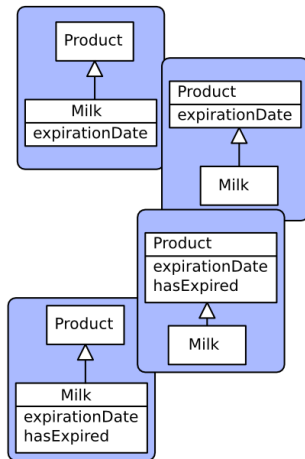
Uncertainty: set of possibilities

Semantics of Partial Models

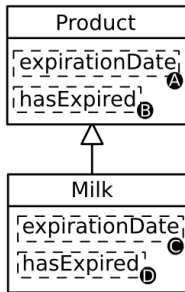


Semantics of Partial Models

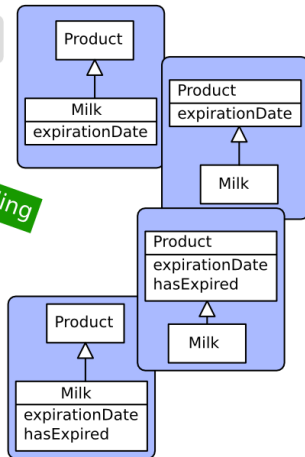
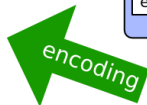
Partial Models:
compact and **exact**
representation
of the set.



Semantics of Partial Models

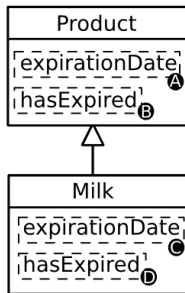


$$(A \leftrightarrow \neg C) \wedge (B \rightarrow A) \wedge (D \rightarrow C)$$



Partial Models:
compact and **exact**
representation
of the set.

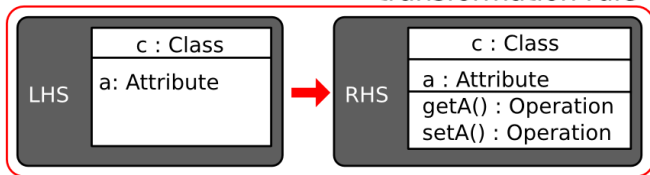
Goal of This Work



$(A \leftrightarrow \neg C) \wedge$
 $(B \rightarrow A) \wedge (D \rightarrow C)$

How can we transform
a Partial Model?

transformation rule



① Introduction

② Partial Models

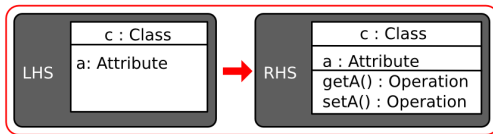
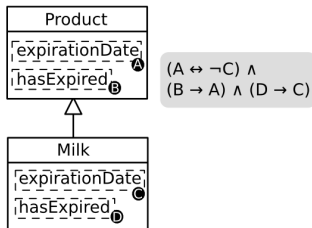
③ Transforming Partial Models

④ “Lifted” Transformation Semantics

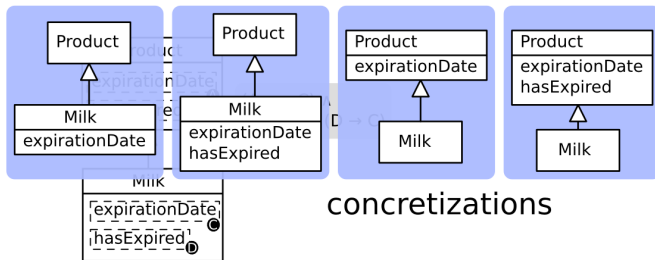
⑤ Checking Lifted Rules

⑥ Conclusion

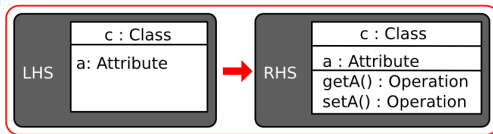
Intuition



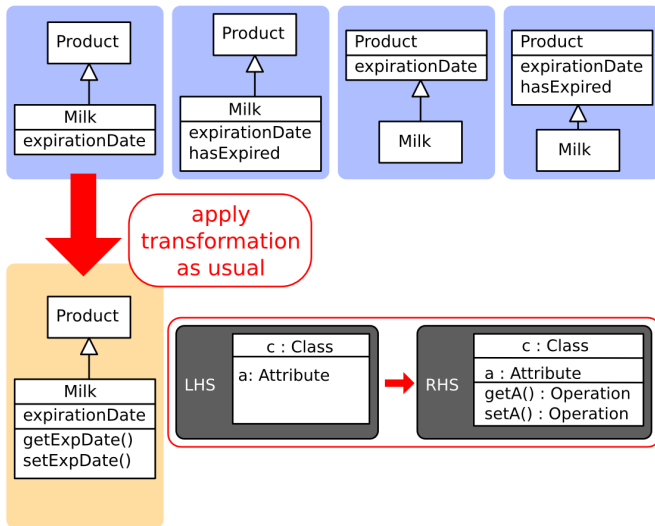
Intuition



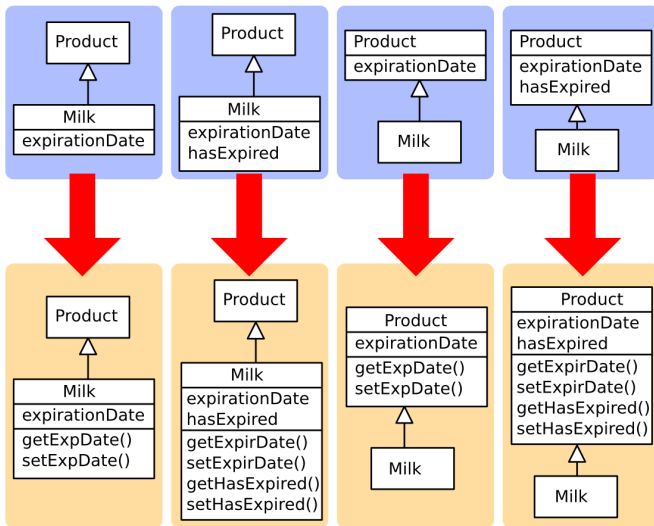
concretizations



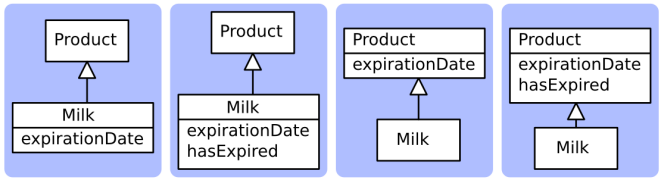
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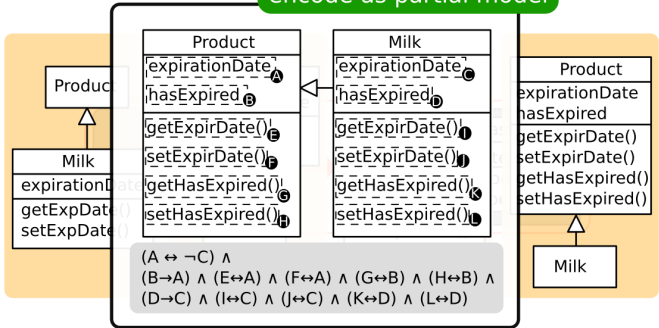
Intuition



Intuition



encode as partial model



Our approach

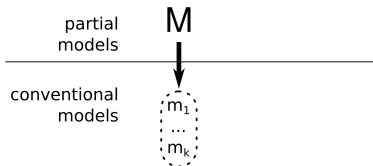
Summarizing the intuition:

$$M \xrightarrow{\mathcal{R}} N$$

Applying a transformation to a partial model M

Our approach

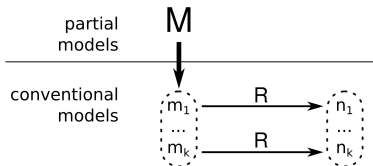
Summarizing the intuition:



Applying a transformation to a partial model M
should be the same as if
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Our approach

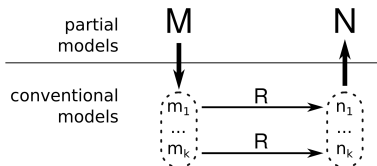
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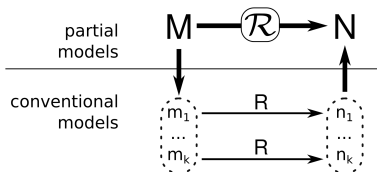
Summarizing the intuition:



Applying a transformation to a partial model M
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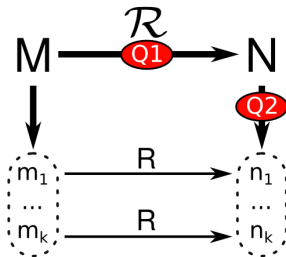
Summarizing the intuition:



Correctness Criterion

Applying a transformation to a partial model M
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applied the transformation to each separately,
and encoded the result as a partial model.

Lifting Transformations

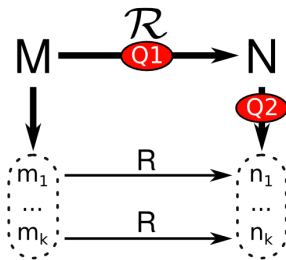


Q1: How do we transform M directly to N ?

Q2: Are the concretizations of N exactly the models $n_1 \dots n_k$?

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Applying Rules to Partial Models



Q1: How do we transform M directly to N ?

- *Lifted semantics* of transformations, using logic.

Q2: Are the concretizations of N exactly the models $n_1 \dots n_k$?

Transfer Predicates

Represent $M \xRightarrow{R^*} N$ as:

$$\Phi_N = \mathcal{R}(R, M, N) \wedge \Phi_M$$

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Conclusion

\mathcal{R} is a conjunction $\phi_1 \wedge \phi_2 \wedge \dots$

- One subformula at each application point:

$$(\Phi_{\text{LHS}} \rightarrow \Phi_{\text{RHS}}) \wedge (\neg \Phi_{\text{LHS}} \rightarrow \Phi_{\text{NE}})$$

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"Left hand side" of the rule;
matching pattern.

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"Right hand side" of the rule;
rule side effect.

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If the rule matches, apply it.

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Represent $M \xrightarrow{R^*} N$ as:

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- One subformula at each application point:

$$(\Phi_{\text{LHS}} \rightarrow \Phi_{\text{RHS}}) \wedge (\neg \Phi_{\text{LHS}} \rightarrow \Phi_{\text{NE}})$$

Rule did not match;
No-Op.

Transfer Predicates

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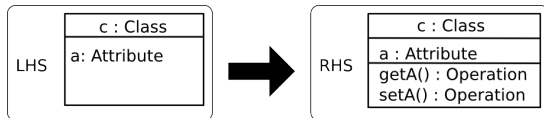
\mathcal{R} is a conjunction $\phi_1 \wedge \phi_2 \wedge \dots$

- One subformula at each application point:

$$(\Phi_{\text{LHS}} \rightarrow \Phi_{\text{RHS}}) \wedge (\neg \Phi_{\text{LHS}} \rightarrow \Phi_{\text{NE}})$$

If the rule does not match,
do nothing.

Example 1/2



$$(\Phi_{LHS} \rightarrow \Phi_{RHS}) \wedge (\neg \Phi_{LHS} \rightarrow \Phi_{NE})$$

- $\Phi_{LHS} = c \wedge a \wedge \neg g \wedge \neg s$
- $\Phi_{RHS} = (c' \leftrightarrow c) \wedge (a' \leftrightarrow a) \wedge (g' \leftrightarrow a) \wedge (s' \leftrightarrow a)$
- $\Phi_{NE} = (x' \leftrightarrow x)$

Example 2/2

After matching, grounding and simplifying:

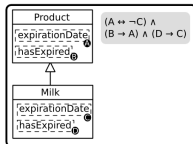
$$\begin{aligned}\mathcal{R}(R, M, N) = & (\text{Product}' \leftrightarrow \text{Product}) \wedge (\text{Milk}' \leftrightarrow \text{Milk}) \wedge \\ & (A' \leftrightarrow A) \wedge (B' \leftrightarrow B) \wedge (C' \leftrightarrow C) \wedge \\ & (D' \leftrightarrow D) \wedge (E' \leftrightarrow A) \wedge (F' \leftrightarrow A) \wedge \\ & (G' \leftrightarrow B) \wedge (H' \leftrightarrow B) \wedge (I' \leftrightarrow C) \wedge \\ & (J' \leftrightarrow C) \wedge (K' \leftrightarrow D) \wedge (L' \leftrightarrow D) \wedge \\ & (\text{gen_Milk_Product}' \leftrightarrow \text{gen_Milk_Product})\end{aligned}$$

$$\Phi_M \quad \wedge \quad \mathcal{R}(R, M, N) \quad = \quad \Phi_N$$

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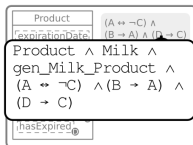


$$\wedge \mathcal{R}(R, M, N) = \Phi_N$$

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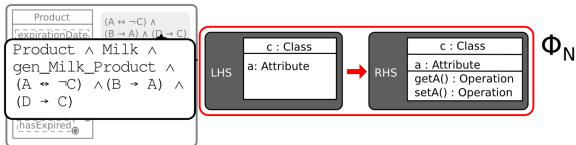
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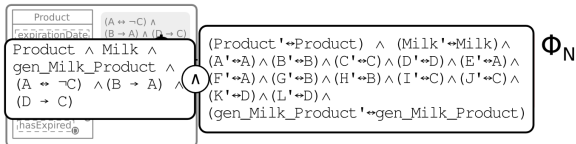
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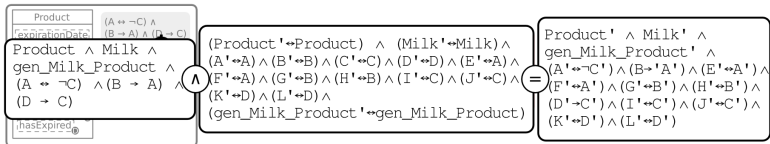
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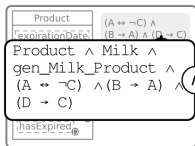
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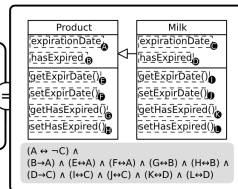
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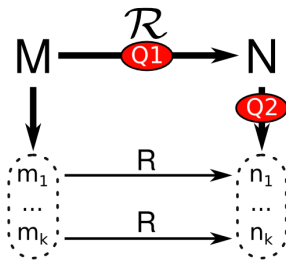


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- 6 Conclusion

Testing Rule Application



Q1: How do we transform M directly to N ?

Q2: Are the concretizations of N exactly the models $n_1 \dots n_k$?

- Check equivalence of encodings using SAT.

Checking Using a SAT Solver

$$\Phi_M \wedge \mathcal{R}(R, M, N) = \Phi_N$$

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Checking Using a SAT Solver

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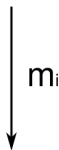
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$$\Phi_{m1}$$

Checking Using a SAT Solver

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$$\Phi_{m1}$$

...

$$\Phi_{mk}$$

Checking Using a SAT Solver

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Partial Models

Lifted
Transform
Semantics

Checking
Lifted Rules

Conclusion

$$\Phi_M \wedge \mathcal{R}(R, M, N) = \Phi_N$$



$$\Phi_{m_1} \wedge \mathcal{R}(R, m_1, n_1) = \Phi_{n_1}$$

...

$$\Phi_{m_k} \wedge \mathcal{R}(R, m_k, n_k) = \Phi_{n_k}$$

Checking Using a SAT Solver

Introduction

Partial Models

Transforming
Partial Models

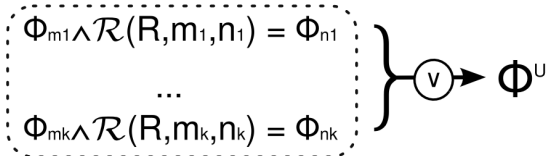
Lifted
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$$\Phi_M \wedge \mathcal{R}(R, M, N) = \Phi_N$$

m_i



Checking Using a SAT Solver

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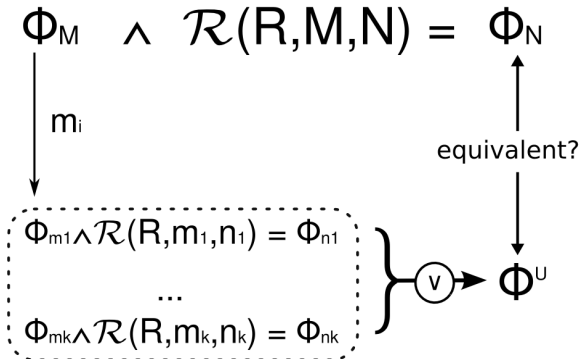
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Checking Using a SAT Solver

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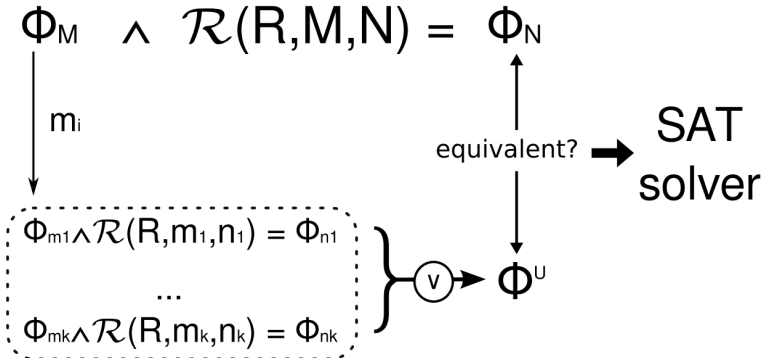
Partial Models

Transforming
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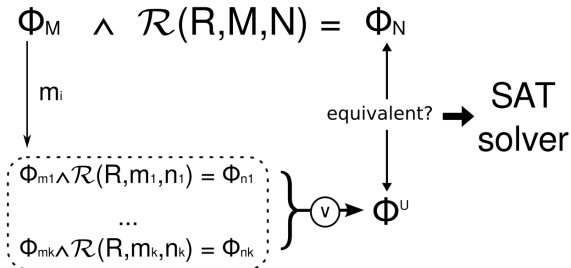
Lifted
Transform
Semantics

Checking
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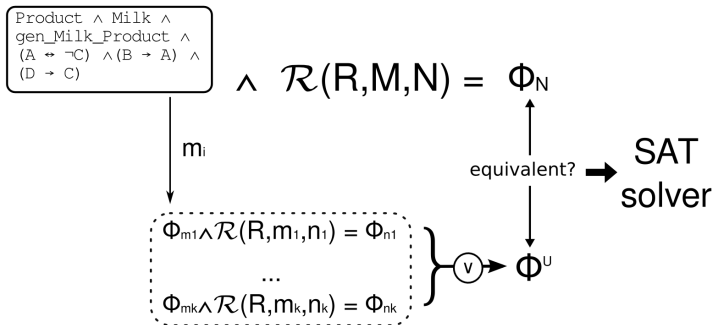
Conclusion



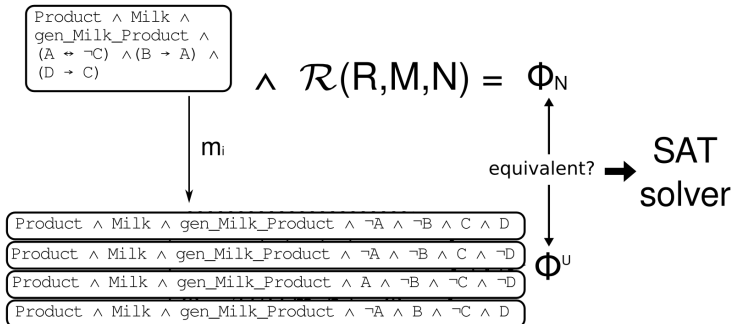
Checking Example



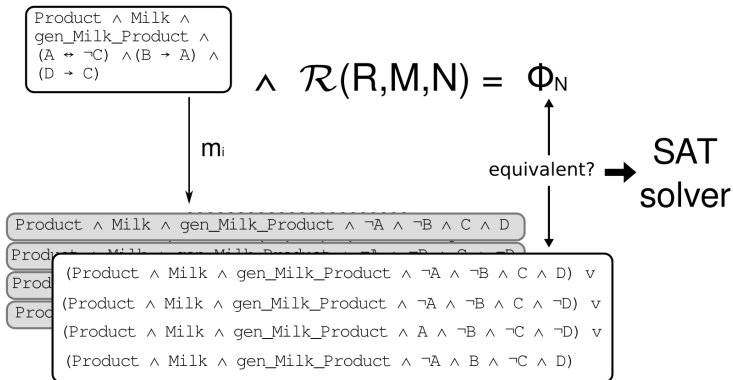
Checking Example



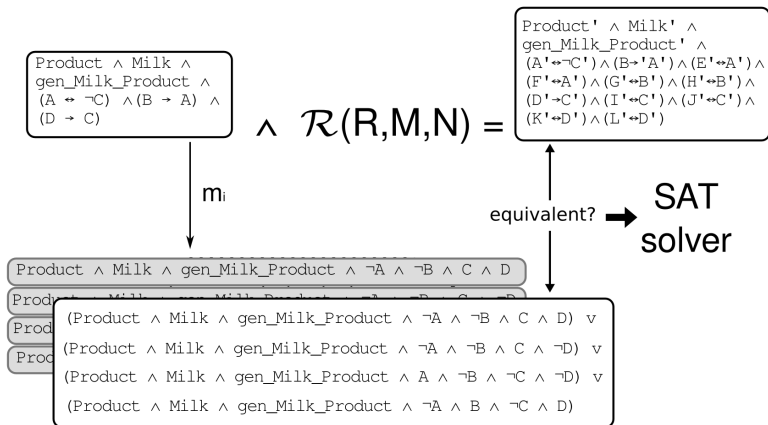
Checking Example



Checking Example

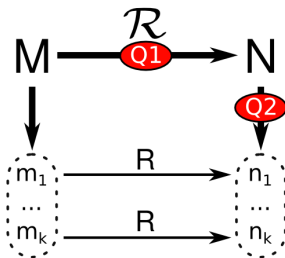


Checking Example



- ① Introduction
- ② Partial Models
- ③ Transforming Partial Models
- ④ “Lifted” Transformation Semantics
- ⑤ Checking Lifted Rules
- ⑥ Conclusion

Summary



Q1: How do we transform M directly to N ?

- *Lifted semantics* of transformations, using logic.

Q2: Are the concretizations of N exactly the models $n_1 \dots n_k$?

- Check equivalence of encodings using SAT.

Conclusion

Transforming models that contain uncertainty.

- Represent uncertainty using Partial Models.
- Lift transformation rules from classical to Partial Models.
- Check Correctness Criterion for the lifted transformation .

Next steps:

- *Compositionally* test Correctness Criterion.
- Systematically create Transfer Predicates using FOL.
- Handle expanding/contracting model vocabularies.
- Partial Models as an Adhesive HLR Category?

Overall research goal [MoDeVVa'11]:

- **Handling uncertainty...**
 - Partial models: *sets of possibilities*.
 - Syntactic “partiality” annotations.
 - Other kinds of partiality (“MAVO”) [FASE'12].
- **...throughout the software lifecycle.**
 - Partial models *as first-class artifacts*.
 - (1) Reasoning [ICSE'12]
 - (2) Refinement [VOLT'12]
 - (3) Transformation

Questions?

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